Density Measurement of Molten Oxides of SiO₂-CaO-Al₂O₃ System by Aerodynamic Levitated Technique

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Abstract

In this study, we measured the density of a molten oxide of SiO_2 -CaO-Al₂O₃ system using Aerodynamic Levitation (ADL) with CO₂-laser heating which can achieve container-less and non-contact conditions for measurements. For density measurements, we improved our ADL system to obtain the appropriate shape for the droplet based on the previously reported system by Langstaff *et al.* We measured the density of molten CaAl₂O₄ between 1600 to 2300K. We conclude that our ADL system has the potential to precisely measure molten oxide density due to good agreement of our density of CaAl₂O₄ with previous data. Using these techniques, we succeeded also to measure the density of a molten SiO₂-CaAl₂O₄ oxide system and discussed the molar volume change by varying the SiO₂ composition.

Keyword(s): Levitation, Thermophysical properties, Density, Molten oxide Received :16 June 2017; Accepted 28 September 2017; Published 31 October 2017

1. Introduction

Density and its temperature dependence on liquid matter is very important for thermophysical property measurements and predictions, however it is difficult to estimate when multiple elements are involved, due to the complexity of volume changes for each individual liquid element. Especially, thermophysical properties, including density of molten oxides, are of great interest in numerous research fields including, steel making, geological science and material science. Molten oxide systems have an extensive range of components and therefore their density is correspondingly difficulty to predict based on chemical composition and temperature. As a result, we must directly and precisely measure the densities of the numerous key components in the molten oxide. However, precisely measuring density of a molten oxide is very difficult due to high temperature and high chemical reactivity. Therefore, previous measurements have been limited to temperatures around 1800K1). To achieve measurements over 1800K, we must use a container-less approach. However, electromagnetic levitation²⁾ cannot be applied due to the low electrical conductivity of the molten oxides. The electrostatic levitation (ESL)³⁾ technique is a possible alternative. However since ESL needs ultra-high vacuum conditions to avoid electric sparks at the electrode, we can use it on the limited molten oxide samples to measure its thermophysical properties. This limitation is the reason of changing the composition of the conditions for the molten oxide due to their high evaporation rate in a vacuum. Previously, the thermophysical properties (density, surface tension and viscosity) of the molten oxides, $Al_2O_3^{(3)}$ and $CaAl_2O_4^{(4)}$ were successfully measured using ESL, due to their low evaporation rate even in vacuum. In order to measure the same properties of more complex compositions of molten oxides, we must use the aerodynamic levitation (ADL) technique⁵⁾. To measure the properties mentioned above using ADL, we improved the levitation gas-jet nozzle unit. For density measurements, we improved our ADL system to obtain the correct shape of the droplet based on the previously reported system by Langstaff *et al.*⁶⁾.

Using our improved conical nozzle system with ADL, we obtained the density of the molten oxides, CaAl2O4 and SiO2-CaAl₂O₄. We obtained the density of molten CaAl₂O₄ with temperature variations from 1600 to 2250K, then using the data we examined the system and procedure using our ADL technique to measure density with temperature variations and compared this with previously reported results⁴⁾⁷). We also tried to measure the multicomponent system of molten oxides using SiO2-CaO-Al₂O₃ in our ADL technique. The SiO₂-CaO-Al₂O₃ is popular in many research fields, and their thermophysical properties have been obtained for limited compositions and temperature. Using our ADL technique, we succeeded to measure the density of a molten SiO₂-CaAl₂O₄ system with various amounts of SiO₂ and also in various temperature range from 1000 to 2600K. From density measurements for the SiO₂-CaO-Al₂O₃ system, we discuss the molar volume change for SiO₂-CaAl₂O₄ and SiO₂-Ca₃Al₂O₆ and compare this with the previous models⁸⁾ derived from measurements in a limited temperature range in a container.

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Fig. 1 Schematics of aerodynamic levitation system for density measurements of molten oxides.

2. Aerodynamic Levitation (ADL) System for Density Measurement of Molten Oxides

The aerodynamic levitation (ADL) technique is a simple method for floating the samples in a gas-jet flow from conical nozzles, which maintains the sample position and is containerless. For levitation of the molten oxide system, we used Ar or dehydrated air for the levitation gas-jet. The gas was selected for stability of the sample and to reduce evaporation. Figure 1 shows a schematic of our ADL system for measuring thermophysical properties based on the previously reported system by Langstaff et al.⁶⁾. A mass-flow controller was used to precisely control the levitation gas-jet flow and to prevent the shape of the drop deviating from a perfect sphere. Spherical solid oxide samples, about 2mm in diameter, were levitated in the gas-jet flow, and then they were melted under the container-less conditions by irradiation from two CO₂ lasers. The sample temperature was measured using a monochromatic pyrometer at a wavelength of 0.9μ m. In the ADL system, we installed an acoustic oscillation system to generate surface oscillations on the levitated droplets in order to measure surface tension and viscosity by the oscillating drop method⁶). Since this report focus the density measurement, the surface oscillation excitation by the acoustic speaker system described in detail in elsewhere⁹⁾.

The density of the molten sample by levitation is obtained by dividing its mass by its volume. The mass can be easily obtained precisely using a balance before and after levitation. The volume of levitated molten sample was obtained from its shape using images of its shadow as lit from the side using a laser system at 532nm, which eliminates radiation from the molten oxide. The shape of ADL droplet is modified along the vertical direction due to gravity and the pressure of the levitation gas-jet flow. We need to improve the nozzle unit for observing half of the full droplet to obtain the volume when it is vertically elongated. Another reason for improving the nozzle unit is for passing a laser beam through the nozzle to the levitated samples from below. This is required to make a homogeneous temperature in the levitated molten oxide using two laser beams from above and below. Conventional

nozzles did not allow the laser beam from below to efficiently penetrated through the nozzle, therefore the laser power was reduced to 70%. To compensate for this, we improved the nozzle unit by implementing a conical shape and modifying the gas-flow path. Due to these improvements, we succeeded in observing the droplet shape over half of the full droplet and homogenized the temperature distribution of the sample by applying the laser from below at 94% power.

3. Observation of Static Shape of ADL Droplet and Density Measurement of Molten CaAl₂O₄

On the ground, the static shape of a 2mm diameter ADL droplet is slightly distorted from a perfect sphere due to gravity. Therefore, we must observe the droplet from the side, using backlighting, to obtain the volume of the droplet from the cross sectional image. **Fig. 2** shows cross sectional images of the ADL molten Al_2O_3 droplet. From **Fig. 2**, we found that the droplet is slightly ellipsoidal in shape due to gravitational distortion. From the shadow images we determined the outline of the droplet and fitted the following ellipsoid equation,

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$
 (1)

where a and b are the horizontal and vertical lengths from the center of mass. For the best fit to the equation, the values of a and b were changed to converge on the minimum of the differences between the outline and the fitting shape. Then we calculated the volume of the droplet, V, assuming the axial symmetry in the direction of gravity as;

$$V = \frac{4\pi}{3}a^2b.$$
 (2)



Fig. 2 Shadow image of molten Al₂O₃ with 2.0mm diameter by backlight laser optics system and fitting curve by ellipsoidal equations.

The density of the droplet can then be obtained by $\rho = m/V$, where m is the mass of the sample, and V is given by eq. (2) above. To examine the change in mass of the sample during the experiments, we measured its mass both before and after the experiments. In the present experiments, the change in mass for all samples was less than 1%. For confirmation of our density measurement system, we measured the density of molten CaAl₂O₄. The molar composition ratio is $CaO:Al_2O_3 = 1:1$ and forms the compound CaAl₂O₄ which has a melting temperature of 1878K and is therefore stable in the liquid phase with very low evaporation rate in high temperature ranges. Due to the stability of CaAl₂O₄, density measurements have already been taken using ESL^{4} and ADL^{7} . Therefore, $CaAl_2O_4$ is a good sample for examining the system and procedure of our ADL techniques for the density measurements. We obtain a value for the density of molten CaAl₂O₄ in a temperature range from 1600 to 2300K. The variation of the density of molten CaAl₂O₄ with temperature is shown in Fig. 3. The uncertainty in this data at each temperature per shadow image is ± 23.2 mg/cm³, using the coverage factor, k = 2. The uncertainty calculations were carried out in the same manner as reported in previous studies using static magnetic field applied electromagnetic levitation facilities 10), which is based on the Guide to Uncertainty of Measurement (GUM)¹¹⁾. Our volume measurements of the ADL droplet used images of a partially obscured droplet, and we had to take into account the uncertainty due to the obscured portion. However, for the present measurements, we did not include the effect of the obscured portion on uncertainly of density measurements, since we confirmed that the droplet was symmetrical in both the horizontal and vertical axes after rapid solidification. However, while measuring the molten sample we were unable to discern the actual shape of the droplet, and future work should consider the accounting for the uncertainly due to the obscured portion of the droplet volume on density measurements.



Figure 3 shows the results of density measurements using container-less techniques by ESL⁴⁾ and ADL⁷⁾. All results for density measurements from several measurements were plotted and they dispersed in the range of ± 23.2 mg/cm³ from the average density values at the corresponding temperature. From **Fig. 3**, we found that our dispersion range of measured densities includes the previous measured results by ESL and ADL. Our data are in good agreement with density values and temperature coefficients from previous results. Our results confirmed that our density measurement system can obtain values for molten oxide density in

temperature ranges exceeding 1800K.

4. Density Measurement of Molten SiO₂-CaO-Al₂O₃ System

Density measurements of various compositions of molten SiO₂-CaO-Al₂O₃ with made using an ADL system. In the present report we focus on the molar volume change with varying amounts of SiO₂ for CaAl₂O₄ and Ca₃Al₂O₆. Since CaAl₂O₄ and Ca₃Al₂O₆ are stable liquids, even at high temperature, we were interested in the molar volume change from adding SiO₂ into these compounds. Courtial and Dingwell⁸⁾ (CD) investigated the molar volume change for these systems. Using the Archimedean method, which measures density by means of weight inserted into liquid samples, they measured the density of four compositions of molten SiO2-Ca3Al2O6. However, for molten SiO₂-CaAl₂O₄ they could only measure the density of two compositions. For SiO₂-CaAl₂O₄, using only three data points; $CaAl_2O_4$, SiO_2 : $CaAl_2O_3 = 1 : 1$ and $SiO_2 = 100 \text{mol}\%$, they predicted a molar volume change from adding SiO₂ to CaAl₂O₄. (Pure SiO₂ data is predicted from extrapolation density data from SiO₂ glass by Bacon et al.¹²⁾, which is not direct measurement data.) Therefore, in order to confirm the molar volume change of this system predicted by CD, we tried to measure the density of many compositions of molten SiO₂-CaAl₂O₄. For these measurements, we processed the following procedures for precisely controlling the compositions of various SiO₂-CaAl₂O₄ melts. The oxide sample preparations are shown in Fig. 4. Initially, we dried powders of SiO₂, CaO and Al₂O₃ at 1173K in oven heaters to evaporate any H2O from the samples. Any H2O present in the sample powders will interfere with the composition adjustments when weighing them. The dried powders of each raw material, CaO, SiO₂ and Al₂O₃, were mixed in the necessary weights for each composition. Then the mixed powders were pressed into a 10mm diameter pellet. These pellets were then cut into 2mm diameter samples to be used in the ADL experiments. The pieces cut from the pellet were levitated in the conical nozzle and made spherical. The spherical samples were aerodynamically levitated and stabilized and the melted samples were uses for the

Fig. 3 Density of molten CaAl₂O₄ with temperature variations.

Name	SiO ₂	Al_2O_3	CaO
0mol%	0	50.0	50.0
9mol%	9.0	45.5	45.5
21mol%	21.2	39.4	39.4
27mol%	26.6	36.7	36.7
41mol%	40.6	29.7	29.7

 Table 1
 Compositions (mol%) of SiO₂-CaAl₂O₄ system for density measurements



Fig. 4 Procedure of oxide sample preparations for density measurements by ADL system.

density measurements. Sample SiO_2 -CaAl₂O₄ compositions for which we could measure density across a wide temperature range, are listed in **Table 1**.

We tried to measure the density of other SiO_2 -CaAl₂O₄ compositions, however for high SiO_2 compositions over 50mol% we could not precisely measure the density over a wide temperature range because of the high evaporation rate of SiO_2 at temperatures exceeding 2800K. In this experiment, for the five compositions mentioned above, we could measure their density and temperature dependence.



Fig. 5 Temperature dependence of molten SiO_2 -CaAl₂O₄ density with composition variation of SiO_2 from 0 to 41mol%.

Using these oxide samples, we measured density using an ADL system. Figure 5 shows the results for density of molten systems with temperature variations. The uncertainty in the density data is ± 23.2 mg/cm³ with the coverage factor, k = 2. This is same as that for the molten CaAl₂O₄ density described in section 3. However, in Fig. 5 we found larger dispersions of density for each composition and temperature. If a coverage factor of k = 3 was used, we could not cover the measured density dispersions. This would be attributed to sample oscillations. Fluctuations in the levitation gas-jet flow generated oscillations in the sample which became larger than those seen in the CaAl₂O₄ measurements. The addition of SiO₂ into CaAl₂O₄ caused large fluctuations in the levitation gas-jet flow, however we were unable to ascertain the reasons for this in this experiment. Therefore, the density data in Fig. 5 was largely dispersed and not centered on a point. For the density data of each composition, the liner temperature dependence of density, $\rho(T) = \rho_0 + \alpha(T - T_m)$, where ρ_0 is the density at melting temperature, α is the temperature coefficient, and $T_{\rm m}$ is melting temperature, was fitted to the density data to obtain the temperature dependence density for each composition. ρ_0 , α and $T_{\rm m}$ for each composition are listed in **Table 2**. From the temperature dependence density we selected the density at 1973K and obtained the molar volume of each composition at this temperature. These molar volumes are plotted against SiO₂ compositions, as shown in Fig. 6. Figure 6 shows the predicted curve for molar volume change of SiO₂-CaAl₂O₄ with SiO₂ compositions along with data measured by CD. Only CD's data and the fitting curve is shown for the SiO₂- Ca₃Al₂O₆ system. Our data is for the SiO₂-CaAl₂O₄ system, and shown with CD's data and the corresponding fitting curve, which was traced from CD's paper⁸⁾. Our data is in good agreement with CD's fitting curve. Therefore, our density measurements are also in good agreement with CD's measurements. Since our data agrees with CD's data, we can now discuss the molar volume change for the SiO₂-CaAl₂O₄ system. CD predicted the molar volume change of the SiO₂-CaO-Al₂O₃ system. They proposed the change in molar volume with SiO₂ composition, V(T), especially for SiO₂-CaAl₂O₄ and SiO₂-Ca₃Al₂O₆,

Sample Name	$e ho_0(\mathrm{kg}\cdot\mathrm{m}^{-3})$ a	$\alpha (\mathrm{kg} \cdot \mathrm{m}^{-3} \cdot \mathrm{T}^{-1})$	$\boldsymbol{T}_{m}\left(K\right)$
0mol%	2.73×10^{-3}	-7.59×10^{-8}	1878
9mol%	2.71×10^{-3}	-6.17×10^{-8}	1847
21mol%	2.78×10^{-3}	-8.21×10^{-8}	1823
27mol%	2.80×10^{-3}	-15.6×10^{-8}	1731
41mol%	2.59×10^{-3}	-5.56×10^{-8}	1714

using the following equation, which was based on the excess molar volume in a SiO₂-CaO system,

$$V(T) = \sum_{i} X_{i} V_{i}(T) + X_{\text{SiO}_{2}} \cdot X_{\text{CaO}} \cdot V_{\text{SiO}_{2}\text{-CaO}}$$
(3)

where X_i and V_i are the mole fraction of oxides, and the partial molar volume of oxides, respectively. *i* denotes components of the system, in this case SiO₂ and CaAl₂O₄, or Ca₃Al₂O₆. Also X_{SiO_2} ; X_{CaO} and V_{SiO_2-CaO} are pseudo binary-composition mole fractions of SiO₂ and CaO, and the molar volume of SiO₂-CaO, respectively. If the molar volume of changes ideally by mixing SiO2 into CaAl2O4 or Ca3Al2O6, which implies no excess volume in eq.(3), we can add a linear line of best fit to the molar volume data for 0 to 100mol% of SiO2. However, in Fig. 6 both systems of the molar volume data did not change linearly, and we also found that they have an excess volume lower than the ideal molar volume, as the fitting line for the molar volume data is below the linear line. Our molar volume data is in good agreement with the fitting curve, similar to CD in which the molar volume of molten SiO₂-CaAl₂O₄ was obtained by subtracting the molar volume of molten SiO₂-CaO⁸⁾ from the ideal molar volume (linear line) of SiO₂-CaAl₂O₄. CD obtained the fitting curve from only three data points. From the agreement of our molar volume data with this curve, we consider the fitting curve correctly shows the molar volume change of the SiO₂-CaAl₂O₄ system.

For the molar volume change of the SiO₂-CaAl₂O₄ system, CD proposed that SiO₂ highly interacts with CaO in CaAl₂O₄ and the molar volume shrinks because of this. Their measured data of molten SiO₂-CaO system showed that the addition of CaO into SiO₂, the molar volume shrank drastically. From these results, CD considered that each component in the SiO2-CaO system highly interact and easily connect with each other. Then for SiO₂-CaAl₂O₄, the molar volume would shrink due to the addition of SiO₂. CD used these concepts to measure the molar volume, V_{SiO2}-CaO, of SiO2-CaO in eq.(3). Also for the SiO2-Ca₃Al₂O₆ system, CD applied the same concept to SiO₂ with CaO for fitting the molar volume data. From the agreement of the fitting curve and molar volumes from the density measurements, CD concluded the in the SiO2-CaAl2O4 and SiO2-Ca3Al2O6 systems, SiO₂-CaO interaction is important for the molar volume change. However, the SiO₂-Al₂O₃ interaction is not a main contributor to the molar volume change. Presently, our molar volume change in the SiO₂-CaAl₂O₄ system assists CD's interaction model of SiO2-CaO in the molar volume change of CaAl2O4 with added SiO₂. However, CD's empirical model is based only on a limited number of measurements, therefore it is necessary to measure more compositions for the SiO₂-CaO-Al₂O₃ system.

From our present measurements and comparisons with other density data for the same samples taken using different measurement techniques, we conclude that our density measurement



Fig. 6 Molar volume change with SiO₂ compositions for SiO₂-CaAl₂O₄ and SiO₂-Ca₃Al₂O₆ at 1973K. Courtial and Dingwell⁸⁾ results were plotted by \Box (SiO₂-CaAl₂O₄) and \blacksquare (SiO₂-Ca₃Al₂O₆).

system using ADL will be effective with molten oxide systems. Therefore, for future work, we will conduct more data for density measurements of a molten SiO₂-CaO-Al₂O₃ system, and based on these results and physical modeling, derive equations that predict molar volume change.

5. Conclusion

We selected the aerodynamic levitation (ADL) technique for molten oxide levitation and density measurements. For the density measurement, we obtained the volume of the ADL droplet from a three-quarters side view of the drop which was distorted due to gravity. We improved the conical nozzle shape for better observation of the images. Using the improved conical nozzle unit we successfully observed the droplet and calculated the density of molten CaAl2O4 and SiO2-CaO-Al2O3 system with temperature variations. Our density data for molten CaAl₂O₄ with temperature variations was in good agreement with previous measured data using ESL and ADL. Therefore we confirmed that our ADL measurement system can be applied to precise density measurements of molten oxide systems. Furthermore, from the density measurement results of SiO2-CaAl2O4 we discussed the molar volume change of SiO2-CaAl2O4 with varying amounts of SiO₂. Our molar volume data was in good agreement with the predictions of Courtial and Dingwell from an empirical evaluation. For future work, we will take many more density measurements of molten SiO₂-CaO-Al₂O₃ systems, and based on these results and physical modeling, derive an equation to predict the molar volume change.

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